CePS₄ Electronic Structure and Optical Properties

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The structure of CePS₄ has been determined from single-crystal X-ray diffraction data $(I4_1/acd \text{ space group}, a = b = 10.9228(3) \text{ Å}, c = 19.3998(6) \text{ Å}, V = 2314.5(2) \text{ Å}^3, Z = 16).$ The refinement, conducted from 547 independent reflections ($I > 3\sigma(I)$ and 30 variables) led to $R_{\rm F}$ (%) = 1.83 and $R_{\rm wF}$ (%) = 2.36. Diffuse reflectance spectra of CePS₄ and of the $La_{1-x}Ce_xPS_4$ series indicated that the electronic absorption mechanism in CePS₄, a 4f¹ \rightarrow $5d^0$ transition on the Ce^{III} ions, is the same as in γ -Ce₂S₃, with only the band gap width being modified. To this transition corresponds an absorption threshold responsible for the yellow hue of the thiophosphate at about 2.5 eV. Band structure calculation (TB-LMTO-ASA) confirms the experimental evidence of the Ce^{III} $4f^1 \rightarrow 5d^0$ transition. Comparisons between CePS₄ and γ -Ce₂S₃ through their electronic localized functions revealed the inductive effect of the P-S covalent bonding on the Ce-S bond, with the resulting increase of the $Ce^{III} 4f^1 \rightarrow 5d^0$ transition in the thiophosphate as compared to the sulfide. This increase is ascribed, in part, to a lowering of the 4f block because of the decreased screening effect of the more ionic Ce-S bonding in CePS₄.

Introduction

In a previous study on the crystal and electronic structure of sodium-doped cerium sulfide $Na_{3x}Ce_{2-x}S_3$ compounds, ¹ it was shown that the red color of these materials was to be attributed to an absorption corresponding to the Ce^{III} atom-like band-based $4f^1 \rightarrow 5d$ electronic transition. The insertion–substitution of alkali-metal (Li, Na, K ...) into the Th₃P₄-type structure of cation deficient γ -Ce₂S₃ (Ce_{8/3} $\Box_{1/3}$ S₄) resulted in a color change of the pristine material, the phase evolving from red-burgundy to bright-red in the $Na_{3x}Ce_{2-x}S_3$ series (0 < x < 0.125), in accord with the overall increased ionicity of the phase.² This color change, related to the widening of the $4f^1 \rightarrow 5d^0$ energy gap by about 0.1 eV, was observed from the threshold energies of the diffuse reflection spectra and from powder photocurrent measurements.³ To study the inductive effect⁴⁻⁷ on the Ce-S bond and its consequences on this particular electronic transition, we decided to turn toward CePS₄ since this phase presents a completly different absorption energy

gap as evidenced by its bright-yellow color.⁸ We thus embarked on the synthesis of this material to determine its optical properties but, because neither its accurate crystal nor its electronic structure were known, an attempt to synthesize single crystals of the phase was first made. We hence report the successful preparation of CePS₄ single crystals and the precise structure determination of the compound, followed by its band structure determination. In addition, numerous compositions of the $La_{1-x}Ce_xPS_4$ solid solution were synthesized to confirm the nature of the optical transition inducing the color of CePS₄, through UV-visible diffuse reflection spectra recording. The electronic structure scheme of the compound has been then studied in relation with its optical properties and by comparison with the γ -Ce₂S₃ phase to explain the chromatic differences between the two materials and to unravel the influence of phosphorus on the Ce 4f-5d energy gap.

Experimental Section

Synthesis of CePS₄ and of the $La_{1-x}Ce_xPS_4$ Series (0 \leq x < 1). CePS₄ and the solid solutions of several La_{1-x}Ce_xPS₄

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Table 1. Crystallographic Data and Experimental Details for CePS₄ Physical and Crystallographic Data

formula: CePS₄ color: yellow system: tetragonal

linear abs coeff:

crystal size (mm³): $0.1 \times 0.1 \times 0.15$ space group: I41/acd (No. 142) cell params (powder refinement, T = 300 K): a = b = 10.9228(3) Å, c = 19.3998(6) Å, V = 2314.5(2) Å³, Z = 16, $d_{calcd} = 3.435$ g cm⁻³

 $\mu(\lambda_{MoK-L2,3}) = 94.97 \text{ cm}^{-1}$

Recording Conditions

diffractometer: CAD4-F

scan mode: ω/θ

molar mass: 299.369

temperature: 293 K radiation: $\lambda_{MoK-L2.3} = 0.71069$ Å monochromator: oriented graphite (002) angular range 2θ (deg): 3.0-70.0standard reflectns: (4 2 4), (4 -2 4), (-4 -2 -4) abs correction: semiempirical based on ψ scans transm coeff: 0.0624 - 0.1156

total recd reflectns: 13112 independent reflections $(I > 3\sigma(I))$: 547 obsd reflectns ($I > 3\sigma(I)$): 2287

Refinement

Data Reduction

weighting scheme: $w = 1/(\sigma^2 |F_0| + (0.01 \times 1.5 |F_0|)^2)$ refinement results (on observed reflections): R(%) = 1.83secondary extinction coefficient: 0.190(8) residual electronic density: $[-0.60, +0.81] e^{-/A^3}$

compounds (0 $\leq x < 1$) were prepared according to the procedure described by Huang⁸ and Le Rolland:^{9,10} finely ground powders of Ce₂S₃ (325 mesh, Cerac, 99.9%), La₂S₃ (-200 mesh, Strem Chemicals, 99.9%), and P₂S₅ (Merk, 99.8%) taken in the aimed stoichiometric ratio were placed in evacuated (10^{-3} Torr) quartz tubes, sealed, and slowly heated at 900 °C for 10 days with an intermediary stage of 2 days at 300 °C. The samples were then slowly cooled to room temperature. All compounds were handled in dry glovebox because of their great air sensitivity. From the very thin microcrystalline powder obtained, CePS₄ single crystals were then prepared by transport at 950 °C with iodine (40 mg of I₂ for a silica tube length of about 15 cm and an inner diameter of 1 cm and around 500 mg of CePS₄) for 10 days. Well-shaped single crystals were then picked up from the sample bulk for crystallographic analyses.

X-ray Structure Determination

CePS₄ Structure Study. X-ray powder diffraction diagrams were recorded on a CPS 120 INEL X-ray powder diffractometer equipped with a monochromatized radiation Cu $K\text{-}L_2$ and a position-sensitive detector calibrated with Na₂Ca₃Al₁₂F₁₄ as standard.¹¹ The powder was sieved at 20 μ m and introduced in a Lindemann capillary ($\phi = 0.1$ mm). From the reported tetragonal cell constants, all the diagram reflections were assigned (hkl) indices, indicating a good purity of the sample at the X-ray diffraction detection threshold. Accurate cell parameters (a = b = 10.9228(3) Å, c = 19.3998(6)Å) were extracted from a full pattern matching refinement (FULLPROF¹²) ($R_p = 3.65\%$, $R_{wp} = 4.79\%$, $R_{exp} = 3.88\%$ and $\chi^2 = 1.52$). These parameters agree well with the previously published ones.8-10

A 0.10 \times 0.10 \times 0.15 mm³ single crystal of CePS₄ was selected and mounted on a CAD4 X-ray diffractometer for room-temperature data collection. The single-crystal data collection conditions are reported in Table 1. The structure was solved using the atomic positions of the well-known \mbox{LnPS}_4 structural type^{13–16} with the JANA98¹⁷ structure determination package. Conventional atomic and anomalous scattering $R_{\rm int}$ (%) = 3.19 (on observed data)

no. of refined params: 30 $R_{\rm w}$ (%) = 2.36; g.o.f. = 0.89 type: isotropic, type I, Lorenzian distribution

Fable 2.	Fractional	l Atomic	Coordinates	and	Equivalent
Isotrop	ic Atomic	Displace	ment Param	eters	of CePS ₄

hkl range: $-5 \le h \le 17, -5 \le k \le 17, -5 \le l \le 31$

atom	X	У	Ζ	$U_{ m eq}$ (Å ²)
Ce(1)	1/2	3/4	5/8	0.0153(3)
Ce(2)	1/2	3/4	3/8	0.0144(3)
Р	3/4	0.7128(1)	1/2	0.0141(5)
S(1)	0.7483(1)	0.8194(1)	0.41396(5)	0.0192(4)
S(2)	0.59348(8)	0.61158(9)	0.50198(6)	0.0165(4)

factors were taken from the usual sources. The diffraction data analysis confirmed the previously reported Laue symmetry and space group (I41/acd). Semiempirical ψ scan-based absorption corrections were made, and after averaging (547 independent reflections, $R_{\rm int} = 3.19\%$), the refinement cycles led to $R_{\rm F} = 1.83\%$, $R_{\rm w} = 2.36\%$, and a goodness of fit of 0.89 (30 variables). The final difference electron density showed features no higher than 0.81 e^{-/A^3} and no lower than -0.60e⁻/Å³. The atomic and equivalent isotropic displacement parameters are gathered in Table 2.

 $La_{1-x}Ce_{x}PS_{4}$ ($0 \le x \le 1$) Compounds Structural Study. For each $La_{1-x}Ce_xPS_4$ compound $(0 \le x \le 1)$, the X-ray powder diffraction pattern was found to present a single phase, demonstrating the occurrence of a random La/Ce distribution. The cell parameters were obtained from a full pattern matching refinement.¹² Figures 1a and 1b show the a and cparameter variation versus *x*. The linear decrease of the cell parameters from LaPS₄ to CePS₄ is in agreement with the lanthanide contraction law.

Optical Measurements. The room-temperature UV/VIS/ NIR diffuse reflectance spectra were recorded on finely ground samples with a Perkin-Elmer Lambda II spectrometer. This instrument was equipped with a 60 mm diameter integrating sphere and computer controlled using the PECOL software. The reflectance versus wavelength measurements were made in the 250-1100 nm range (i.e., from about 1.1 to 5.0 eV) using BaSO₄ powder (Perkin-Elmer standard) as reference (100% reflectance). These diffuse reflectivity spectra may be used to obtain values for the band gap which agree rather well with

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Figure 1. *a* and *c* parameter variations versus *x* in the $La_{1-x}Ce_xPS_4$ series. The linear decrease with x is in agreement with the lanthanide contraction law and proves the La/Ce substitution.

those obtained from single crystals. The absorption (α/S) data were calculated from the reflectance using the Kubelka-Munk function:^{18–20} $\alpha/S = (1 - R)^2/2R$, where R is the reflectance at a given energy, α is the absorption coefficient, and *S* is the scattering coefficient. The latter has been shown to be practically energy independent for particle size larger than 5 μ m, which is smaller than the particle size of the samples used here. The band gap was determined as the intersection point between the energy axis at the absorption offset and the line extrapolated from the linear portion of the absorption edge in the α/S versus *E* (eV) plot. Figure 2 gathers the spectra of samples of the $La_{1-x}Ce_xPS_4$ series (x = 0, 0.005, 0.01, 0.05, 0.1, 0.4, and 1).

Band Structure Calculations. The self-consistent ab initio band structure calculations were performed on γ -Ce₂S₃ and CePS₄ with the tight binding linear muffin-tin orbital method in the atomic-sphere approximation (TB-LMTO-ASA).^{21,22} The von Barth-Hedin local exchange correlation potential²³ and the scalar relativistic approximation²⁴ were used. The space was filled with slightly overlapping Wigner-Seitz (WS) atomic spheres and additional interstitial (or empty) spheres. The optimum radii and positions of these spheres were calculated according to the method described by Jepsen and Andersen.²⁵ However, as γ -Ce₂S₃ and CePS₄ are not close-packed compounds, this calculation step was done with great care. The number of additional empty spheres was first adapted in order to have reasonably big Ce spheres (the calculation was not possible with Ce sphere radii bigger than

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Figure 2. α/S versus energy spectra in the 1.1–5.0 eV range for some $La_{1-x}Ce_xPS_4$ samples: (0) x = 0, (1) x = 0.005, (2) x = 00.01, (3) x = 0.05, (4) x = 0.1, (5) x = 0.4, and (6) x = 1).

2.1 Å). The maximum size of the empty spheres was then limited for a more accurate Madelung energy. Finally, a maximum overlap restriction of 16% was applied between the atomic spheres. To take into account the lacunar occupancy of the Ce sites in γ -Ce₂S₃ (in fact Ce_{8/3} $\Box_{1/3}$ S₄), the calculations were performed in the lower symmetry I4 space group (instead of $I\overline{4}3d$ for the Th₃P₄ structural type), conducting to a primitive unit cell of composition Ce₅S₈. The atomic parameters used for the calculation are given for γ -Ce₂S₃ and CePS₄ for reference.26,27

The full LMTO basis set consisted of the 6s, 6p, 5d, and 4f orbitals for Ce spheres, the 3s, 3p, and 3d orbitals for P and S spheres, and the s, p, and d orbitals for empty spheres (ES). For the eigenvalue problem, the following minimal basis set, obtained using the Löwdin downfolding technique,²⁸ was used: the LMTO of Ce (6s, 5d, and 4f), P (3s and 3p), S (3s and 3p), and ES (1s). The *k*-space integration was performed with the tetrahedron method²⁹ and the charge self-consistency was reached with 58 and 13 irreducible k-points for γ -Ce₂S₃ and CePS₄, respectively.

For CePS₄, bonding information was obtained by computing the crystal orbital Hamiltonian population (COHP)³⁰ which is the weighted Hamiltonian population density of states. As recommended by Boucher et al.,³¹ the basis set used for the COHP calculation was the minimal basis set previously mentioned in which all the empty spheres LMTO's have also been downfolded. In addition, the effect of polarization of phosphorus on the electronic cloud was examined with the help of the representation of the electronic density and of the electronic localized function (ELF). This function introduced by Becke and Edgecombe,³² following the works by Lennard-Jones,³³ reveals the degree of pairing of the electrons. The

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⁽²⁶⁾ Since γ -Ce₂S₃ is a phase with a disordered cationic distribution, an ordered arrangement has been considered. It consisted of a C5S8 ordered phase. Data used for the band structure calculations are as follows, Space group $I\overline{4}$, atomic sphere radii (Å) and positions: Ce1 (1.86//0; 0; 0), Ce2 (1.86//1/8; 1/4; 5/8), S1 (1.49//0.3231; 0.9269; 0.0519), S2 (1.49//0.1769; 0.9269; 0.6981). Empty sphere radii (Å) and positions: E1 (1.89//0; 1/2; 1/4), E2 (1.22//0; 0; 1/2), E3 (1.22//1/2; 0; 1/4), E4 (1.22; 1/4; 1/8; 7/8)

⁽²⁷⁾ For the band structure calculations on CePS₄, the data were as follows. Atomic sphere radii (Å): Ce1 (2.00), Ce2 (1.97), P (1.19), S1 (1.18), S2 (1.18). Empty sphere radii (Å) and positions: E1 (1.31// 0.0961; 0.3445; 0), E2 (1.27// 0.2118; 0.0382, 1/8), E3 (1.26//1/4; 0.0329; 1/2), E4 (1.26//0.0204; 0.0139; 0.4296), E5 (1.06//0.2055; 0.3954; 0.1697), E6 (0.96//0.1120; 0.0664; 0.3250), E7 (0.77//0.1804; 0.1621; 0.0726), E8 (0.68//0.3389; 0.1127; 0.1458), E9 (0.58//0.1582; 0.0320; 0.2168).

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Figure 3. CePS₄ structure can be considered as made up from [CeS₈] edge sharing chains (left) sharing corners with neighboring chains along *a* and *b* (middle). Phosphorus cations lie inside [S₄] tetrahedra sharing edges with four adjacent [CeS₈] polyhedra (right).

Table 3. Main Bond Distances (Å) and Angles (deg) in

Ce(1) environment		Ce(2) environment			
Ce(1) - S(1)	2.950(1) (×4)	Ce(2)-S(1)	2.916(1) (×4)		
Ce(1)-S(2)	3.004(1) (×4)	Ce(2)-S(2)	3.065(1) (×4)		
P environment					
P-S(1)	2.035(1) (×2)	S(1) - P - S(1)	110.20(8)		
P-S(2)	2.036(1) (×2)	S(1) - P - S(2)	108.57(5) (×2)		
		S(1) - P - S(2)	107.62(5) (×2)		
		S(2)-P-S(2)	114.25(8)		

ELF is normalized and found between 0 and 1. If paired electrons with antiparallel spins are localized at an *r* point in the direct space, the ELF at *r* tends to 1. This can thus be seen as corresponding to paired electrons of a covalent bond, or of valence lone pairs. In a homogeneous gas, ELF = 0.5.

Results and Discussions

Structural Aspects. No particular discussion is to be made of the CePS₄ structure since the xenotime structural type has been previously reported for other lanthanide phases.^{13–16} In this one case, the structural characteristics are those expected (see Table 3), in agreement with the ionic radii and the charge balance: Ce^{III}P^V(S^{-II})₄. The structure can be considered as constructed from [CeS₈] bicapped prisms and of [PS₄] tetrahedra. Through edge sharing, the [CeS₈] groups constitute, along *c*, infinite chains (Figure 3a). These chains, in turn, share corners with neighboring chains along *a* and *b* to constitute a three-dimensional array (Figure 3b). Phosphorus cations lie inside [S₄] tetrahedron sites resulting from the assembly of two infinite chains (Figure 3c). It results that one [PS₄] tetrahedron shares its edges with those of four [CeS₈] polyhedra of two adjacent chains. The feature relevant to this study (see below) lies in the sulfur atoms being linked to 2 Ce and 1 P.

Optical Properties. To get some insight on the origin of the bright yellow color exhibited by CePS₄, our investigations began by measuring the optical properties of this compound through diffuse reflectance experiments. The obtained α/S vs energy spectrum of CePS₄ (Figure 2, sample 6) shows a steep and well-defined absorption threshold around 2.5 eV, followed by a second one around 3.4 eV. The first steep absorption threshold indicates a good purity of the material, confirming the powder X-ray diffraction data analysis (see above). From the Kubelka–Munk treatment, we can conclude



Figure 4. Proposed band scheme for γ -Ce₂S₃ at 77 K (energy in eV) from transitions observed through photoconductivity (PC), absorption (Abs), and fluorescence (A and B) experiments.³

the insulating nature of CePS₄ with a large energy gap of 2.48 eV. Such a value corresponds to an optical absorption in the blue, resulting in a yellow pigmentation of the material. The second absorption is located in the UV region and, indeed, does not contribute to the chromatic properties of CePS₄. Notice the occurrence of a characteristic shoulder in the first threshold, a shoulder originating in the $2F^{5/2}$ and $2F^{7/2}$ spectroscopic terms associated to the 4f¹ electronic configuration of Ce^{III}.

The red color of γ -Ce₂S₃ (energy gap of \approx 1.89 eV)³ is due to the symmetry and spin-allowed interband, intrasite transition $Ce^{III}-4f^1 \rightarrow Ce^{III}-5d^0$, while the $S^{2-}(sp)$ \rightarrow Ce(5d) indirect and direct charge transfers were found by optical measurement on a single crystal respectively at 2.75 and 3.3 eV in the UV domain.³⁴ Figure 4 highlights the main band features and electronic transition of γ -Ce₂S₃. With the same cerium sulfur surrounding, a similar mechanism must be involved in CePS₄. To confirm this hypothesis, the evolution of the absorption threshold when going from LaPS₄ to CePS₄, i.e., by substituting the Ce^{III} f¹ optically active species to La^{III} (4f⁰, 5d⁰) in the colorless LaPS₄ matrix, has been studied. The results of this study are shown in Figure 2 for the seven compounds corresponding to x = 0, 0.005, 0.01, 0.05, 0.1, 0.4, and 1. For LaPS₄

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Figure 5. Colors presented by some $La_{1-x}Ce_xPS_4$ solid solutions: (0) $LaPS_4$ (x = 0), (2) x = 0.005, (3) x = 0.01, (4) x = 0.05, (5) x = 0.4, and (6) $CePS_4$ (x = 1).

itself, the energy threshold value is found at 3.41 eV, in good agreement with a colorless material: this absorption corresponds to the valence band (vb) \rightarrow conduction band (cb) electronic transition. For values of x between 0.005 and 0.1 (curves 1, 2, 3, and 4 in Figure 2), an intense and well-defined absorption peak appears around 3.1 eV that can only be attributed to the introduction of the 4f¹ levels of Če^{III} and to the 4f¹ \rightarrow 5d⁰ transition. The positions in energy of these absorption maxima remain quite constant for the low cerium concentrations. For x = 0.4, a small shift of the absorption peak is recorded with a maximum slightly below 3.10 eV: this may be attributed to a more important contribution of the Ce^{III} 5d⁰ levels to the transition. Incidentally, this demonstrates that the 5d levels of La and Ce are not energetically very different, as can also be deduced from the fact that the initial absorption edge of LaPS₄ is not substantially shifted by the substitution. At the same time, a more and more important absorption threshold develops at lower energy, its position for x = 0.4 being close to that of CePS₄. These observations show clearly that the yellow color of CePS₄ is due to the important $4f^1 \rightarrow cb$ transition of Ce^{III}, the yellow hue being due mostly to the position of the absorption edge itself. In effect, and as can be seen from the color pictures taken for the $La_x Ce_{1-x} PS_4$ series (Figure 5), the samples with x =0.005 and 0.01 (samples 2 and 3) appear white-cream in relation with an absorption beginning at around 2.6 eV and having a maximum at 3.1 eV. As soon as the concentration reaches x = 0.05 (sample 4), the absorption edge is found at 2.55 eV due to the widening of the 3.1 eV band. For x = 0.4 (sample 5) the visual appearance of the phase is practically that of CePS₄ itself. This study thus confirms that the electronic absorption mechanism in γ -Ce₂S₃ and CePS₄ is the same, only the bandwidth being substantially modified. It is this modification whose origin is now going to be evidenced.

Band Structure Calculations. If the absorption process involved in the color of cerium sulfides appears as well established, the energy separation between the Ce-f and Ce-d block, responsible of the color variation, remains difficult to predict. However, a qualitative approach, through the concept of inductive effect as proposed by Etourneau et al.⁷ can be considered to evaluate the trend to be expected in the energy gap changes. Thus, the inductive effect of phosphorus on

Table 4. Observed and Calculated Transition Energies in γ -Ce₂S₃ and CePS₄ (This Work and References 3 and 34)

	γ -Ce _{2S3}			CePS ₄	
	obsd		calcd	obsd	calcd
$\begin{array}{c} 4f^1 \rightarrow cb \\ vb \rightarrow cb \end{array}$	1.89 ³ 2.75 (in 3.3 (dire	direct) ³⁴ ect) ³⁴	1.36 2.94	2.48 3.41	1.00 3.26
5		N INNI I	W/menelydy/		
0					
inergy (eV)		No.	A Manager		
ш		all		s	Ce
-10 -					-
г Г	 N	10 20 30) 20 0	5 10

Figure 6. Band structure of γ -Ce₂S₃ along the more dispersed directions and total density of state (DOS) and DOS projected along the different elements.

sulfur must induce a higher ionic character of the Ce–S bond in CePS₄ compared with γ -Ce₂S₃, explaining a change in color from red to yellow. Band structure comparisons between these two phases have been done in order to approach more quantitatively the charge redistribution between sulfur and cerium versus the effect of the phosphorus–sulfur bonding.

Concerning γ -Ce₂S₃, even though the band structure has been extensively discussed before,^{2,35} we thought it necessary to recalculate it in order to more easily compare its features with those of CePS₄. In Figures 6 and 7 are presented the band structure of γ -Ce₂S₃ and CePS₄, respectively (along the most dispersed direction), the total density of state (DOS) and the density of state projected along the different elements. The calculations show that, in both cases, the top of the vb is sulfur 3p in character whereas the bottom of the cb is essentially based on the 5d orbitals of cerium. The 4f block (1/14th filled) is situated between the vb and cb blocks (see Table 4). The energy needed to add an electron on a Ce^{III} site is estimated at about 6 eV (Hubbart energy) and this explains why the $4f \rightarrow 5d$ transfer mechanism takes place instead of a vb \rightarrow 4f¹ or an intersite 4f¹ + $4f^1 \rightarrow 4f^0 + 4f^2$ one.^{36–39} Owing to the highly localized character of the 4f orbitals, and the highly repulsive effect between the intra-cerium 4f electrons, the 4f nondispersed bands cannot lead to any metallic conductivity. Indeed, the calculations agree well with an observed wide-gap semiconducting behavior.

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Figure 7. Band structure of $CePS_4$ along the more dispersed directions and total density of state (DOS) and DOS projected along the different elements.



Figure 8. COHP of $CePS_4$: (a) evolution of the COHP versus energy of the P–S mean bonding. (b and c) Ce–S interactions within the anionic bands.

Now the role of the phosphorus cation present in CePS₄ on the electronic structure can be addressed, with respect to the relative position of the vb, cb, and 4f levels. Figure 8a gives, for CePS₄, the evolution versus energy of the COHP of the P-S mean bonding. It shows that all the bands situated below -5 eV correspond to a bonding character of the P-S interaction. These bands are little dispersed because the [PS₄] groups are isolated from each other by ionic Ce-S bond barriers (see Figure 3), implying that the system could be as well described, as far as the phosphorus groups are concerned, by a molecular orbital scheme rather than by an electronic band one. From this viewpoint, Figure 9 represents a theoretical hybridization scheme of the s and p orbitals of phosphorus and sulfur in the T_d point symmetry. In this scheme are clearly found the four groups of molecular orbitals in which P-S bonding character and positions are in perfect agreement with the (P-S) COHP function of CePS₄ (Figure 8a). It is also worth noticing that 8 out of 12 p orbitals of the sulfur atoms of the isolated [PS₄] units have a nonbonding character toward phosphorus but are involved in cerium-sulfur bonding interactions (see below). This character is easily observed in the CePS₄ band structure



Figure 9. Theoretical hybridization scheme of the s and p orbitals of phosphorus and sulfur in the T_d point symmetry. Nonbonding 1 e, 3 t₂, and 1 t₁ orbitals (see Figure 8) are those engaged in the Ce–S bonds.

since in the [-5, 0] eV energy range the projected phosphorus DOS is practically equal to zero, whereas it is maximum in the projected cerium DOS (Figure 7).

Considering now the Ce – S interactions within the anionic bands (Figures 8b and 8c), one can observe that the Ce atoms give rise to a contribution in the [-20, -1] eV range. Since, with respect to γ -Ce₂S₃, a part of these valence bands is stabilized through the interaction of sulfur atoms with phosphorus (the S-p block ranges from -2.26 to -10.73 eV in CePS₄ and from -1.58 to -5.16 eV in γ -Ce₂S₃), it ensues that the electrons engaged in cerium–sulfur bonds are more localized on sulfur in the thiophosphate, showing the inductive effect of phosphorus.

The result of the more ionic Ce-S bond is a decrease of the vb and cb dispersion calculated when going from γ -Ce₂S₃ to CePS₄: the bandwidths are of ca. 3.6 and 5.1 eV, respectively, for γ -Ce₂S₃, whereas they are equal to ca. 2.9 and 4.7 eV, respectively, for CePS₄ (see Table 4). This results in a change of the vb/cb energy gap (2.94 eV in γ -Ce₂S₃ and 3.26 eV in CePS₄), in agreement with the experimental data (single crystals measured indirect gap E_i of about 2.75 eV and direct gap E_g of about 3.3 eV for γ -Ce₂S₃ and powder measured gap of 3.41 eV for CePS₄). Concerning the 4f/cb gap, the calculations give an energy of 1.36 and 1.00 eV for γ -Ce₂S₃ and CePS₄, respectively, in contradiction to the experimental observations (see optical section), the 4f/cb gap being wider for CePS₄ than for γ -Ce₂S₃. It is well-known that the calculations cannot, to date, localize reliably the 4f levels. This means that we can only suggest an origin for the enhancement of the $4f^1 \rightarrow cb$ gap width from the binary to the ternary phase; this suggestion is based on the characteristics found for the vb and cb.

On going from red γ -Ce₂S₃ to yellow CePS₄, a 0.59 eV 4f/cb energy difference increase is needed. Even if we consider that the 0.32 eV vb/cb shift is, in one way or another, entirely passed on the 4f \rightarrow 5d gap, we have to assume that a 4f level energy decrease takes place. This lowering can very well take place owing to the decrease of the cerium 4f screening of the nucleus charge because of the increase of the Ce \rightarrow S charge transfer from γ -Ce₂S₃ to CePS₄, upon the phosphorus inductive action.

To confirm this effect of the P–S bonding, two types of relevant data can be considered: the electronic density and the ELF. In γ -Ce₂S₃ we observe the occurrence of a very good sphericity of the electron clouds around the chalcogen atoms. In CePS₄ the same electronic distributions are strongly delocalized toward the phosphorus atoms because of the very strong covalent P–S interaction, whereas a rather regular feature is maintained on the cerium side. A stronger electronic localization is observed on the sulfur atoms in CePS₄ with an ELF_{max} of 0.95 compared to γ -Ce₂S₃ with an ELF_{max} of 0.90 assigned to a higher lone pair localization in CePS₄ that asserts a higher ionic character of the cerium–sulfur bond in the thiophosphate.

Conclusion

The chromatic properties of CePS₄ have been determined and compared to those of the γ -Ce₂S₃. Band structure calculations assert that the origin of color in both materials is a 4f-Ce \rightarrow 5d-Ce electronic transition. Moreover, the color shift from red for the cerium sulfide to yellow for the thiophosphate has been explained in terms of a negative inductive effect of phosphorus, i.e., a reinforcement of the ionic character of the Ce-S bond under the effect of a main group element. The higher the ionicity of the Ce–S bond, the higher the 4f-Ce \rightarrow 5d-Ce energy gap. A similar phenomena was at work in Eu²⁺-doped BaLiF₃ and BaSiF₆^{7,40} where the decrease in energy of the $4f^7 \rightarrow 4f^65d^1$ transition in the former was correlated to an increase of the Eu-F covalency. Nevertheless, even if the inductive effect is a generally understood concept which may be used broadly to better target new synthetic works, band structure calculations are requested to reach a more quantitative approach of the influence on the material properties of the covalency of a bond.

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Supporting Information Available: Crystal structure report consisting of a observed powder pattern, tables of atomic coordinates and anisotropic atomic displacements, and a listing of observed and calculated structure factors (8 pages). Ordering information is given on any current masthead page.

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